### So far...

- Discussed deadlocks, conditions for deadlocks to happened, mechanisms to prevent deadlock and mechanisms to avoid deadlocks
  - Avoiding deadlocks means that you don't go into an unsafe state



# Banker's Algorithm

- Multiple instances of resources
- ▶ Each process must a priori claim the maximum amounts of resources to use.
- When a process requests a resource it may have to wait
  - When a process gets all its resources it must return them in a finite amount of time



### Data Structures for the Banker's Algorithm

Let n = number of processes, and m = number of resources types

- ▶ Available: Vector of length m. If available [j] = k, there are k instances of resource type R<sub>j</sub> available.
- Max: n x m matrix. If Max [i,j] = k, then process P<sub>i</sub> may request at most k instances of resource type R<sub>j</sub>.
- Allocation: n x m matrix. If Allocation[i,j] = k then P<sub>i</sub> is currently allocated k instances of R<sub>j.</sub>
- Need: n x m matrix. If Need[i,j] = k, then P<sub>i</sub> may need k more instances of R<sub>j</sub> to complete its task.

Need[i,j] = Max[i,j] - Allocation[i,j].



# Safety Algorithm

1. Let *Work* and *Finish* be vectors of length *m* and *n*, respectively. Initialize:

Work = Available  
Finish 
$$[i]$$
 = false for  $i = 0,1, ..., n-1$ 

- 2. Find an *i* such that both:
  - (a) Finish [i] = false
  - (b)  $Need_i \leq Work$

If no such *i* exists, go to step 4.

- 3.  $Work = Work + Allocation_i$  Finish[i] = truego to step 2.
- 4. If *Finish* [*i*] == true for all *i*, then the system is in a safe state.



### Resource-Request Algorithm for Process $P_i$

Request = request vector for process  $P_i$ . If Request<sub>i</sub>[j] = k then process  $P_i$  wants k instances of resource type  $R_i$ .

- 1. If *Request<sub>i</sub>* ≤ *Need<sub>i</sub>* go to step 2. Otherwise, raise error condition, since process has exceeded its maximum claim.
- 2. If  $Request_i \le Available$ , go to step 3. Otherwise  $P_i$  must wait, since resources are not available.
- 3. Pretend to allocate requested resources to  $P_i$  by modifying the state as follows:

```
Available = Available - Request<sub>i</sub>;
Allocation<sub>i</sub> = Allocation<sub>i</sub> + Request<sub>i</sub>;
Need<sub>i</sub> = Need<sub>i</sub> - Request<sub>i</sub>;
```

- $\lambda$  If safe  $\Rightarrow$  the resources are allocated to Pi.
- λ If unsafe ⇒ Pi must wait, and the old resource-allocation state is restored



# Example of Banker's Algorithm

- ▶ 5 processes *P*<sub>0</sub> through *P*<sub>4</sub>; 3 resource types *A*(10 instances), *B*(5 instances) and *C*(7 instances)
- $\triangleright$  Snapshot at time  $T_0$ :

	<u>Allocation</u>	<u>Max</u>	<u>Available</u>
	ABC	ABC	ABC
$P_0$	010	753	3 3 2
P	200	322	
P	302	902	
P	3 211	222	
P	4 002	4 3 3	



# Example (Cont.)

▶ The content of the matrix. Need is defined to be Max – Allocation.

$$\frac{Need}{ABC}$$
 $P_0$  743
 $P_1$  122
 $P_2$  600
 $P_3$  011
 $P_4$  431

The system is in a safe state since the sequence  $\langle P_1, P_3, P_4, P_2, P_0 \rangle$  satisfies safety criteria.



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# Example $P_1$ Request (1,0,2) (Cont.)

Check that Request ≤ Available (that is, (1,0,2) ≤ (3,3,2) ⇒ true.

$\angle$	\ <i>llocation</i>	<u>Need</u>	<u>Available</u>
	ABC	ABC	ABC
$P_0$	010	7 4 3	230
$P_1$	302	020	
$P_2$	3 0 1	600	
$P_3$	211	0 1 1	
$P_4$	002	4 3 1	

- Executing safety algorithm shows that sequence<P1, P3, P4, P0, P2> satisfies safety requirement.
- ▶ Can request for (3,3,0) by P4 be granted?
- ▶ Can request for (0,2,0) by P0 be granted?



### **Deadlock Detection**

- Allow system to enter deadlock state
- Detection algorithm
- Recovery scheme

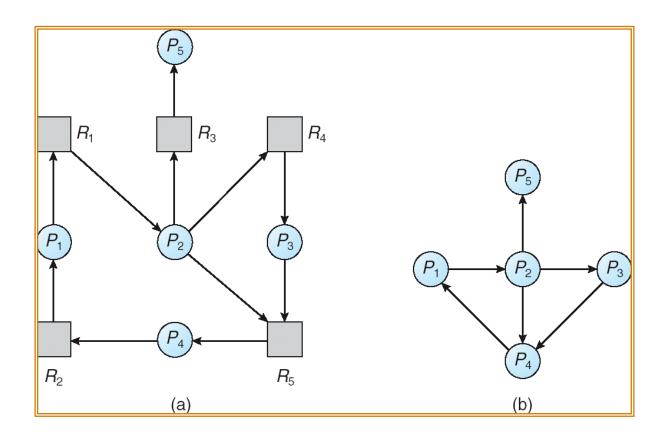


# Single Instance of Each Resource Type

- Maintain wait-for graph
  - Nodes are processes.
  - $P_i \rightarrow P_j$  if  $P_i$  is waiting for  $P_j$ .
- Periodically invoke an algorithm that searches for a cycle in the graph.
- An algorithm to detect a cycle in a graph requires an order of  $n^2$  operations, where n is the number of vertices in the graph.



# Resource-Allocation Graph and Wait-for Graph





Resource-Allocation Graph

Corresponding wait-for graph

# Several Instances of a Resource Type

- ▶ Available: A vector of length m indicates the number of available resources of each type.
- ▶ Allocation: An n x m matrix defines the number of resources of each type currently allocated to each process.
- Request: An n x m matrix indicates the current request of each process. If Request [i<sub>j</sub>] = k, then process P<sub>i</sub> is requesting k more instances of resource type. R<sub>j</sub>.



# **Detection Algorithm**

- 1. Let *Work* and *Finish* be vectors of length *m* and *n*, respectively Initialize:
  - (a) Work = Available
  - (b) For i = 0,1, ..., n-1, if allocation<sub>i</sub>  $\neq 0$ , then Finish[i] = false;otherwise, Finish[i] = true.
- 2. Find an index *i* such that both:
  - (a) Finish[i] == false
  - (b)  $Request_i \leq Work$ If no such i exists, go to step 4.
- 3. Work = Work + Allocation; Finish[i] = true go to step 2
- 4. If Finish[i] == false, for some i,  $1 \le i \le n$ , then the system is in deadlock state. Moreover, if Finish[i] == false, then  $P_i$  is deadlocked.



# **Example of Detection Algorithm**

- Five processes P₀ through P₄; three resource types A (7 instances), B (2 instances), and C (6 instances).
- $\triangleright$  Snapshot at time  $T_0$ :

#### Allocation Request Available

$$ABC$$
  $ABC$   $ABC$   $ABC$   $P_0$  010 000 000  $P_1$  200 202  $P_2$  303 000  $P_3$  211 100  $P_4$  002 002

Sequence  $P_0$ ,  $P_2$ ,  $P_3$ ,  $P_4$  will result in Finish[i] = true for all i



# Example (Cont.)

 $\triangleright$   $P_2$  requests an additional instance of type C.

Request

ABC

 $P_0 \, 000$ 

 $P_1$  201

 $P_2 = 0.01$ 

 $P_3$  100

 $P_4 002$ 

- State of system?
  - Can reclaim resources held by process  $P_0$ , but insufficient resources to fulfill other processes; requests.
  - Deadlock exists, consisting of processes  $P_1$ ,  $P_2$ ,  $P_3$ , and  $P_4$ .



# **Detection-Algorithm Usage**

- When, and how often, to invoke depends on:
  - How often a deadlock is likely to occur?
  - How many processes will need to be rolled back?
    - one for each disjoint cycle
- If detection algorithm is invoked arbitrarily, there may be many cycles in the resource graph and so we would not be able to tell which of the many deadlocked processes "caused" the deadlock.



### Recovery from Deadlock: Process Termination

- Abort all deadlocked processes
- Abort one process at a time until the deadlock cycle is eliminated
- In which order should we choose to abort?
  - Priority of the process
  - How long process has computed, and how much longer to completion
  - Resources the process has used.
  - Resources process needs to complete.
  - How many processes will need to be terminated.
  - Is process interactive or batch?



### Recovery from Deadlock: Resource Preemption

- Selecting a victim minimize cost.
- Rollback return to some safe state, restart process for that state.
- Starvation same process may always be picked as victim, include number of rollback in cost factor.

